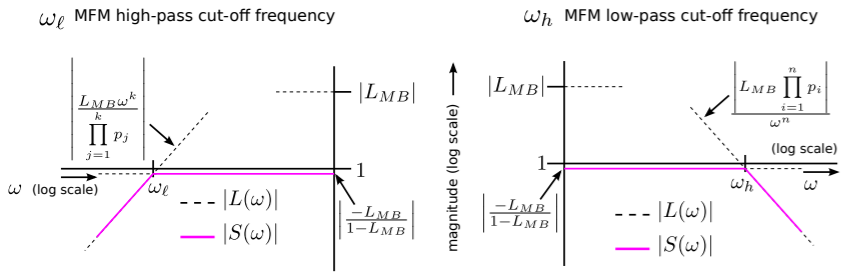


# Frequency compensation techniques

## Bandwidth definition of a feedback amplifier



After the design of the bandwidth the poles of the transfer are generally not in MFM positions.

Use the root-locus technique to find the poles of the servo function from the poles, the zeros and the mid-band frequency value of the loop gain.

## Phantom zero compensation

Zeros can be inserted into loop gain to modify the root locus. Loop gain zeros in the transmission band also appear in the servo function.

A low-pass MFM response is an all-pole response. Servo function may have zeros but transfer must have an all-pole response.

## Second order

Second order MFM transfer  $F_2(s) = \frac{1}{1+s\sqrt{2}/\omega_h+s^2/\omega_h^2}$

### Case: no compensation required

Loop gain with two poles:

$$L(s) = \frac{L_{MB}}{(1-s/p_1)(1-s/p_2)}$$

Servo function:

$$S_2(s) = \frac{L_{MB}}{1-L_{MB}} \frac{1}{1-s/p_1} \frac{1}{1-s/p_2}$$

Low-pass MFM cut-off frequency:

$$\omega_h^2 = (1-L_{MB})p_1p_2$$

No compensation required if the magnitude of the sum of the poles of the loop gain equals sqrt(2) times the low-pass cut-off frequency:

$$p_1 + p_2 = -\sqrt{2}\omega_h$$

### Case: compensation with one phantom zero

Loop gain with two poles and one zero:

$$L(s) = L_{MB} \frac{1-s/z_1}{(1-s/p_1)(1-s/p_2)}$$

Low-pass MFM cut-off frequency:

$$\omega_h^2 = (1-L_{MB})p_1p_2$$

Sum of the poles of the servo function:

$$p_0 + p_1 = p_1 + p_2 - \frac{p_1p_2}{z_1}$$

Conditions for MFM compensation:

$$-p_1 - p_2 < \sqrt{2}\omega_h$$

Phantom zero frequency:

$$z = -\frac{\omega_h^2}{\sqrt{2}\omega_h + p_1 + p_2}$$

## Third order

Third order MFM transfer:

$$F_3(s) = \frac{1}{1+2s/\omega_h+2s^2/\omega_h^2+s^3/\omega_h^3}$$

### No compensation required

Loop gain with three poles:

$$L(s) = L_{MB} \frac{1}{(1-s/p_1)(1-s/p_2)(1-s/p_3)}$$

Servo function:

$$S_3(s) = \frac{L_{MB}}{1-L_{MB}} \frac{1}{1-s/p_1} \frac{1}{1-s/p_2} \frac{1}{1-s/p_3}$$

Low-pass MFM cut-off frequency:

$$\omega_h = \sqrt[3]{(1-L_{MB})p_1p_2p_3}$$

No compensation required if:

$$p_1p_2 + p_1p_3 + p_2p_3 = 2\omega_h^2$$

$$p_1 + p_2 + p_3 = -2\omega_h$$

### Compensation with one phantom zero

Loop gain with three poles and one zero:

$$L(s) = L_{MB} \frac{1-s/z_1}{(1-s/p_1)(1-s/p_2)(1-s/p_3)}$$

Low-pass MFM cut-off frequency:

$$\omega_h = \sqrt[3]{(1-L_{MB})p_1p_2p_3}$$

Conditions for MFM compensation:

$$p_1p_2 + p_1p_3 + p_2p_3 < 2\omega_h^2$$

Phantom zero frequency:

$$z_1 = \frac{\omega_h^3}{p_1p_2 + p_1p_3 + p_2p_3 - 2\omega_h^2}$$

### Compensation with two phantom zeros

Loop gain with three poles and two zeros:

$$L(s) = L_{MB} \frac{(1-s/z_1)(1-s/z_2)}{(1-s/p_1)(1-s/p_2)(1-s/p_3)}$$

Low-pass MFM cut-off frequency:

$$\omega_h = \sqrt[3]{(1-L_{MB})p_1p_2p_3}$$

Conditions for MFM compensation:

$$p_1 + p_2 + p_3 - \frac{p_1p_2p_3}{z_1z_2} = -2\omega_h$$

$$p_1p_2 + p_1p_3 + p_2p_3 - L_{MB}p_1p_2p_3 \left( \frac{1}{z_1} + \frac{1}{z_2} \right) = 2\omega_h^2$$

Phantom zero frequencies:

$$z_1 + z_2 = \frac{\omega_h^3}{p_1 + p_2 + p_3 + 2\omega_h}$$

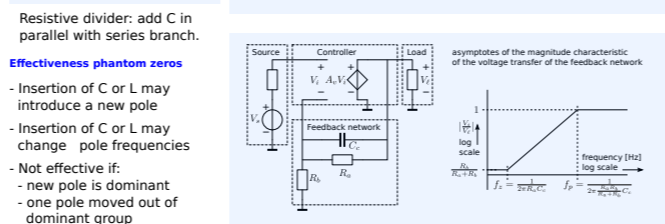
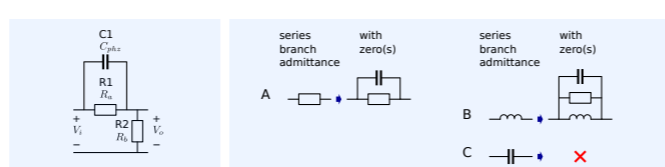
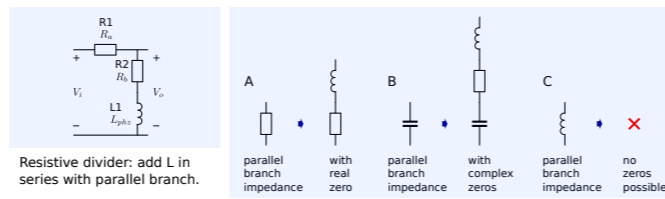
$$z_1 + z_2 = \frac{p_1p_2 + p_1p_3 + p_2p_3 - 2\omega_h^2}{p_1 + p_2 + p_3 + 2\omega_h}$$

## Implementation of phantom zeros

Phantom zero coincides with pole in the ideal gain: cannot be implemented in the controller.

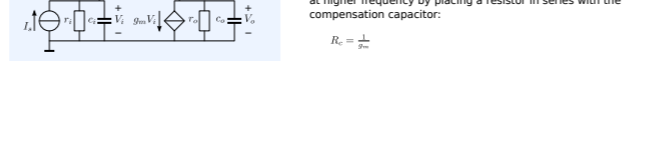
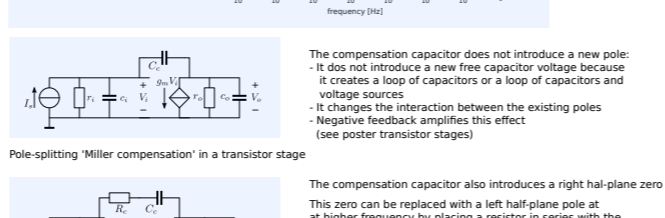
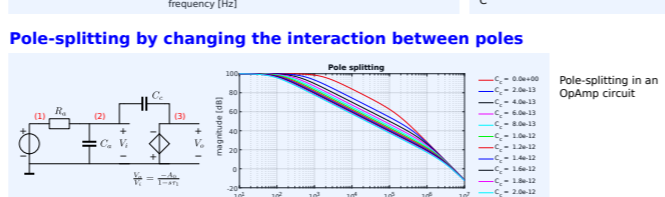
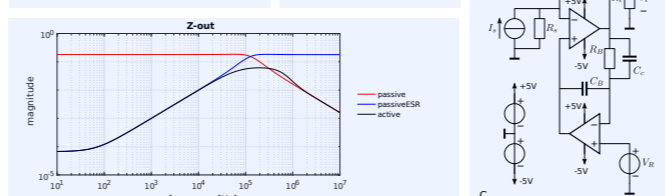
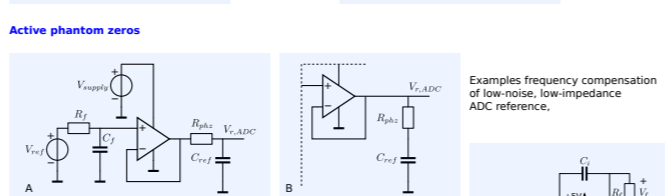
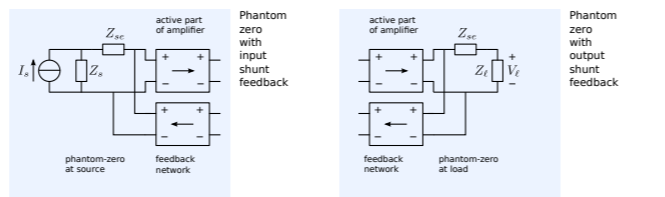
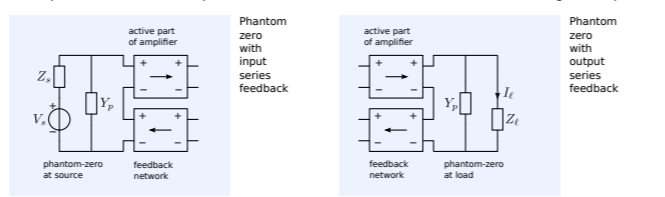
### Passive phantom zeros in feedback network

If the feedback network causes an attenuation in the loop gain, at the frequency that corresponds with that of the phantom zero, this attenuation can be reduced for higher frequencies.

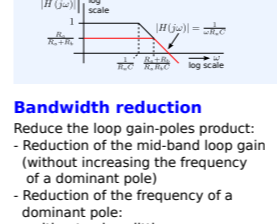
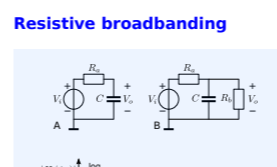
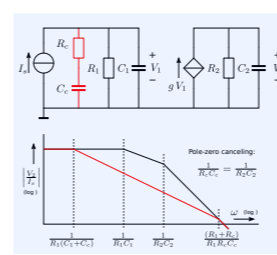


### Passive phantom zeros at the source

If the source/load impedance causes an attenuation in the loop gain, at the frequency that corresponds with that of the phantom zero, this attenuation can be reduced for higher frequencies.

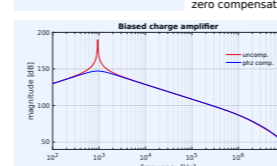
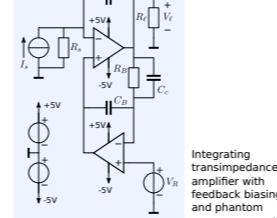
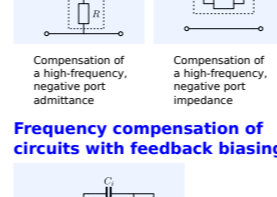
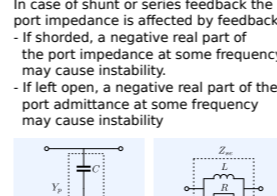
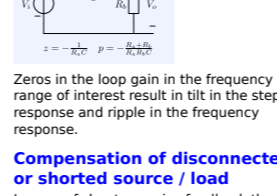
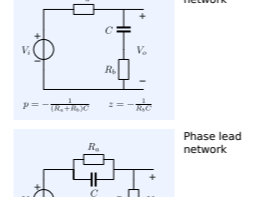
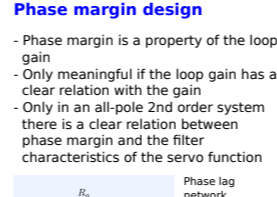


## Pole-splitting through pole-zero canceling

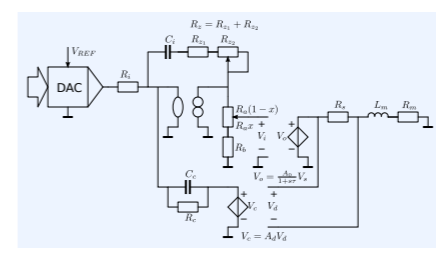


### Bandwidth reduction

Reduce the loop gain-poles product: - Reduction of the mid-band loop gain (without increasing the frequency of a dominant pole) - Reduction of the frequency of a dominant pole: - without pole splitting - with excessive pole-splitting: a pole is moved out of the dominant group



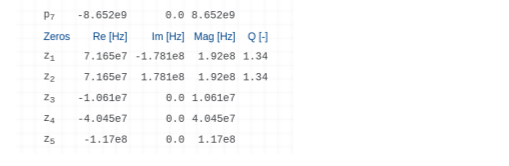
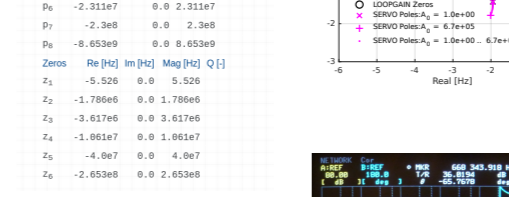
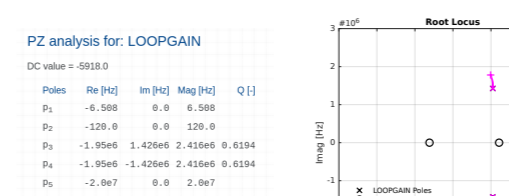
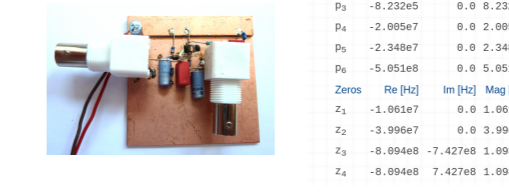
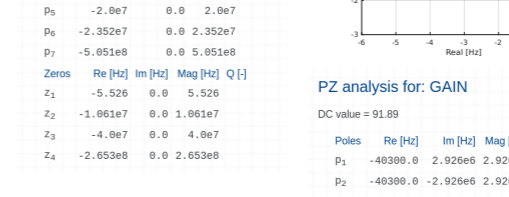
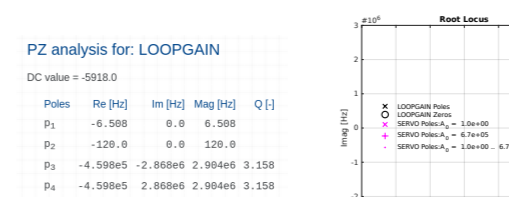
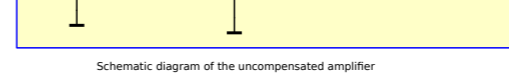
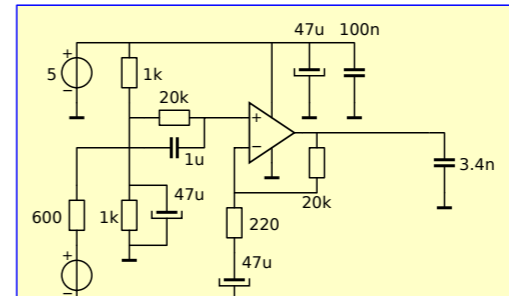
## Analog PID controllers



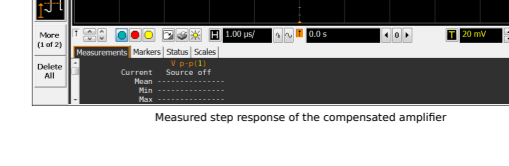
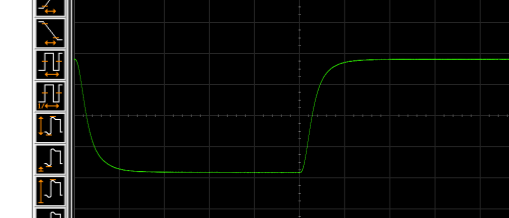
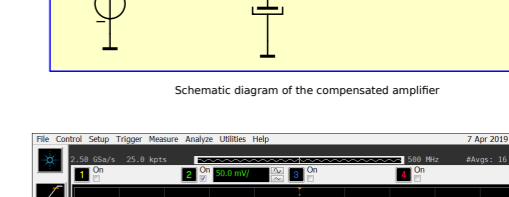
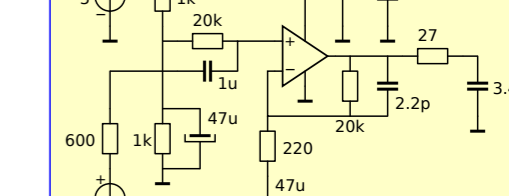
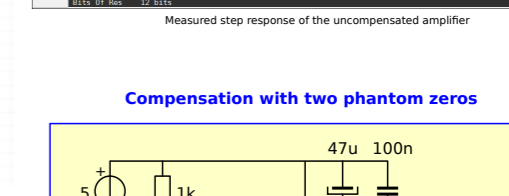
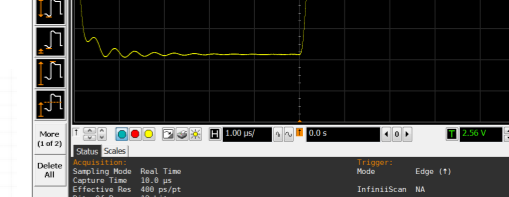
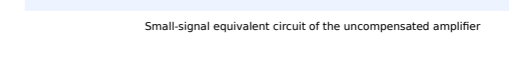
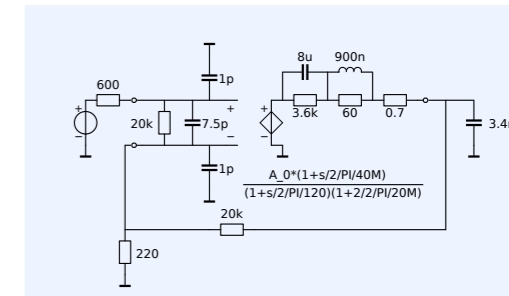
Concept of a motor current driver with PI controller and phantom zero compensation

## Example frequency compensation voltage amplifier for capacitive load

### Uncompensated



(c) 2021 Anton Montagne  
anton@montagne.nl  
https://www.analog-electronics.eu



### Compensation with two phantom zeros

